

उत्तरमाला

प्रश्नावली 7.1

1. $-\frac{1}{2}\cos 2x$
2. $\frac{1}{3}\sin 3x$
3. $\frac{1}{2}e^{2x}$
4. $\frac{1}{3a}(ax+b)^3$
5. $-\frac{1}{2}\cos 2x - \frac{4}{3}e^{3x}$
6. $\frac{4}{3}e^{3x} + x + C$
7. $\frac{x^3}{3} - x + C$
8. $\frac{ax^3}{3} + \frac{bx^2}{2} + cx + C$
9. $\frac{2}{3}x^3 + e^x + C$
10. $\frac{x^2}{2} + \log|x| - 2x + C$
11. $\frac{x^2}{2} + 5x + \frac{4}{x} + C$
12. $\frac{2}{7}x^{\frac{7}{2}} + 2x^{\frac{3}{2}} + 8\sqrt{x} + C$
13. $\frac{x^3}{3} + x + C$
14. $\frac{2}{3}x^{\frac{3}{2}} - \frac{2}{5}x^{\frac{5}{2}} + C$
15. $\frac{6}{7}x^{\frac{7}{2}} + \frac{4}{5}x^{\frac{5}{2}} + 2x^{\frac{3}{2}} + C$
16. $x^2 - 3\sin x + e^x + C$
17. $\frac{2}{3}x^3 + 3\cos x + \frac{10}{3}x^{\frac{3}{2}} + C$
18. $\tan x + \sec x + C$
19. $\tan x - x + C$
20. $2 \tan x - 3 \sec x + C$
21. C
22. A

प्रश्नावली 7.2

1. $\log(1+x^2) + C$
2. $\frac{1}{3}(\log|x|)^3 + C$
3. $\log|1+\log x| + C$
4. $\cos(\cos x) + C$
5. $-\frac{1}{4a}\cos 2(ax+b) + C$
6. $\frac{2}{3a}(ax+b)^{\frac{3}{2}} + C$
7. $\frac{2}{5}(x+2)^{\frac{5}{2}} - \frac{4}{3}(x+2)^{\frac{3}{2}} + C$
8. $\frac{1}{6}(1+2x^2)^{\frac{3}{2}} + C$
9. $\frac{4}{3}(x^2+x+1)^{\frac{3}{2}} + C$
10. $2\log|\sqrt{x}-1| + C$
11. $\frac{2}{3}\sqrt{x+4}(x-8) + C$

12. $\frac{1}{7}(x^3-1)^{\frac{7}{3}} + \frac{1}{4}(x^3-1)^{\frac{4}{3}} + C$ 13. $-\frac{1}{18(2+3x^3)^2} + C$
14. $\frac{(\log x)^{1-m}}{1-m} + C$ 15. $-\frac{1}{8} \log|9-4x^2| + C$ 16. $\frac{1}{2}e^{2x+3} + C$
17. $-\frac{1}{2e^{x^2}} + C$ 18. $e^{\tan^{-1}x} + C$ 19. $\log(e^x + e^{-x}) + C$
20. $\frac{1}{2} \log(e^{2x} + e^{-2x}) + C$ 21. $\frac{1}{2} \tan(2x-3) - x + C$
22. $-\frac{1}{4} \tan(7-4x) + C$ 23. $\frac{1}{2}(\sin^{-1}x)^2 + C$
24. $\frac{1}{2} \log|2\sin x + 3\cos x| + C$ 25. $\frac{1}{(1-\tan x)} + C$
26. $2\sin\sqrt{x} + C$ 27. $\frac{1}{3}(\sin 2x)^{\frac{3}{2}} + C$ 28. $2\sqrt{1+\sin x} + C$
29. $\frac{1}{2}(\log \sin x)^2 + C$ 30. $-\log|1+\cos x| + C$ 31. $\frac{1}{1+\cos x} + C$
32. $\frac{x}{2} - \frac{1}{2} \log|\cos x + \sin x| + C$ 33. $\frac{x}{2} - \frac{1}{2} \log|\cos x - \sin x| + C$
34. $2\sqrt{\tan x} + C$ 35. $\frac{1}{3}(1+\log x)^3 + C$ 36. $\frac{1}{3}(x+\log x)^3 + C$
37. $-\frac{1}{4} \cos(\tan^{-1}x^4) + C$ 38. D
39. B

प्रश्नावली 7.3

1. $\frac{x}{2} - \frac{1}{8} \sin(4x+10) + C$ 2. $-\frac{1}{14} \cos 7x + \frac{1}{2} \cos x + C$
3. $\frac{1}{4} \left[\frac{1}{12} \sin 12x + x + \frac{1}{8} \sin 8x + \frac{1}{4} \sin 4x \right] + C$

4. $-\frac{1}{2}\cos(2x+1)+\frac{1}{6}\cos^3(2x+1)+C$ 5. $\frac{1}{6}\cos^6 x-\frac{1}{4}\cos^4 x+C$
6. $\frac{1}{4}\left[\frac{1}{6}\cos 6x-\frac{1}{4}\cos 4x-\frac{1}{2}\cos 2x\right]+C$
7. $\frac{1}{2}\left[\frac{1}{4}\sin 4x-\frac{1}{12}\sin 12x\right]+C$ 8. $2\tan\frac{x}{2}-x+C$
9. $x-\tan\frac{x}{2}+C$ 10. $\frac{3x}{8}-\frac{1}{4}\sin 2x+\frac{1}{32}\sin 4x+C$
11. $\frac{3x}{8}+\frac{1}{8}\sin 4x+\frac{1}{64}\sin 8x+C$ 12. $x-\sin x+C$
13. $2(\sin x+x\cos\alpha)+C$ 14. $-\frac{1}{\cos x+\sin x}+C$
15. $\frac{1}{6}\sec^3 2x-\frac{1}{2}\sec 2x+C$ 16. $\frac{1}{3}\tan^3 x-\tan x+x+C$
17. $\sec x-\operatorname{cosec} x+C$ 18. $\tan x+C$
19. $\log|\tan x|+\frac{1}{2}\tan^2 x+C$ 20. $\log|\cos x+\sin x|+C$
21. $\frac{\pi x}{2}-\frac{x^2}{2}+C$ 22. $\frac{1}{\sin(a-b)}\log\left|\frac{\cos(x-a)}{\cos(x-b)}\right|+C$
23. A 24. B

प्रश्नावली 7.4

1. $\tan^{-1} x^3 + C$ 2. $\frac{1}{2}\log\left|2x+\sqrt{1+4x^2}\right|+C$
3. $\log\left|\frac{1}{2-x+\sqrt{x^2-4x+5}}\right|+C$ 4. $\frac{1}{5}\sin^{-1}\frac{5x}{3}+C$
5. $\frac{3}{2\sqrt{2}}\tan^{-1}\sqrt{2}x^2+C$ 6. $\frac{1}{6}\log\left|\frac{1+x^3}{1-x^3}\right|+C$

7. $\sqrt{x^2-1} - \log|x+\sqrt{x^2-1}| + C$ 8. $\frac{1}{3}\log|x^3+\sqrt{x^6+a^6}| + C$
9. $\log|\tan x + \sqrt{\tan^2 x + 4}| + C$ 10. $\log|x+1+\sqrt{x^2+2x+2}| + C$
11. $\frac{1}{6}\tan^{-1} \frac{3x+1}{2} + C$ 12. $\sin^{-1} \frac{x+3}{4} + C$
13. $\log|x-\frac{3}{2}+\sqrt{x^2-3x+2}| + C$ 14. $\sin^{-1} \frac{2x-3}{\sqrt{41}} + C$
15. $\log|x-\frac{a+b}{2}+\sqrt{(x-a)(x-b)}| + C$
16. $2\sqrt{2x^2+x-3} + C$ 17. $\sqrt{x^2-1} + 2\log|x+\sqrt{x^2-1}| + C$
18. $\frac{5}{6}\log|3x^2+2x+1| - \frac{11}{3\sqrt{2}}\tan^{-1} \frac{3x+1}{\sqrt{2}} + C$
19. $6\sqrt{x^2-9x+20} + 34\log|x-\frac{9}{2}+\sqrt{x^2-9x+20}| + C$
20. $-\sqrt{4x-x^2} + 4\sin^{-1} \frac{x-2}{2} + C$
21. $\sqrt{x^2+2x+3} + \log|x+1+\sqrt{x^2+2x+3}| + C$
22. $\frac{1}{2}\log|x^2-2x-5| + \frac{2}{\sqrt{6}}\log\left|\frac{x-1-\sqrt{6}}{x-1+\sqrt{6}}\right| + C$
23. $5\sqrt{x^2+4x+10} - 7\log|x+2+\sqrt{x^2+4x+10}| + C$
24. B 25. B

प्रश्नावली 7.5

1. $\log \frac{(x+2)^2}{|x+1|} + C$ 2. $\frac{1}{6}\log\left|\frac{x-3}{x+3}\right| + C$
3. $\log|x-1| - 5\log|x-2| + 4\log|x-3| + C$

4. $\frac{1}{2} \log|x-1| - 2 \log|x-2| + \frac{3}{2} \log|x-3| + C$
5. $4 \log|x+2| - 2 \log|x+1| + C$ 6. $\frac{x}{2} + \log|x| - \frac{3}{4} \log|1-2x| + C$
7. $\frac{1}{2} \log|x-1| - \frac{1}{4} \log(x^2+1) + \frac{1}{2} \tan^{-1} x + C$
8. $\frac{2}{9} \log \left| \frac{x-1}{x+2} \right| - \frac{1}{3(x-1)} + C$ 9. $\frac{1}{2} \log \left| \frac{x+1}{x-1} \right| - \frac{4}{x-1} + C$
10. $\frac{5}{2} \log|x+1| - \frac{1}{10} \log|x-1| - \frac{12}{5} \log|2x+3| + C$
11. $\frac{5}{3} \log|x+1| - \frac{5}{2} \log|x+2| + \frac{5}{6} \log|x-2| + C$
12. $\frac{x^2}{2} + \frac{1}{2} \log|x+1| + \frac{3}{2} \log|x-1| + C$
13. $-\log|x-1| + \frac{1}{2} \log(1+x^2) + \tan^{-1} x + C$
14. $3 \log|x+2| - \frac{5}{x-2} + C$ 15. $\frac{1}{4} \log \left| \frac{x-1}{x+1} \right| - \frac{1}{2} \tan^{-1} x + C$
16. $\frac{1}{n} \log \left| \frac{x^n}{x^n+1} \right| + C$ 17. $\log \left| \frac{2-\sin x}{1-\sin x} \right| + C$
18. $x + \frac{2}{\sqrt{3}} \tan^{-1} \frac{x}{\sqrt{3}} - 3 \tan^{-1} \frac{x}{2} + C$ 19. $\frac{1}{2} \log \frac{x^2+1}{x^2+3} + C$
20. $\frac{1}{4} \log \left| \frac{x^4-1}{x^4} \right| + C$ 21. $\log \left(\frac{e^x-1}{e^x} \right) + C$
22. B 23. A

प्रश्नावली 7.6

1. $-x \cos x + \sin x + C$ 2. $-\frac{x}{3} \cos 3x + \frac{1}{9} \sin 3x + C$
3. $e^x (x^2 - 2x + 2) + C$ 4. $\frac{x^2}{2} \log x - \frac{x^2}{4} + C$